Astronomy & Astrophysics manuscript no. September 24, 2004
(DOI: will be inserted by hand later)

VLTI/VINCI diameter constraints on the evolutionary status of δ Eri, ξ Hya, η Boo

F. Thévenin[1], P. Kervella[2], B. Pichon[1], P. Morel[1], E. Di Folco[3], and Y. Lebreton[4]

[1] Laboratoire Cassiopée, UMR 6202 CNRS, Observatoire de la Côte d'Azur, BP 4229, 06304 Nice Cedex 4, France

[2] Laboratoire d'Etudes Spatiales et d'Instrumentation Astrophysique (LESIA), UMR 8109 du CNRS, Observatoire de Paris, Section de Meudon, 5 place Jules Janssen, 92195 Meudon Cedex, France

[3] European Southern Observatory, Karl-Schwarzschild Strasse 2, D-85748 Garching, Germany

[4] GEPI, UMR 8111 CNRS, Observatoire de Paris, Section de Meudon, 5 place Jules Janssen, 92195 Meudon Cedex, France

Received ; Accepted

Abstract. Using VLTI/VINCI angular diameter measurements, we constrain the evolutionary status of three asteroseismic targets: the stars δ Eri, ξ Hya, η Boo. Our predictions of the large mean frequency spacing of these stars are in agreement with published observational estimations. Looking without success for a companion of δ Eri we doubt on its classification as a RS CVn star.

1. Introduction

After two years of operation, the instrument demonstration VINCI of the VLTI has provided valuable stellar diameter measurements. Among the impact of these diameters are the studies of main sequence stars where diameters combined with asteroseismic frequencies can be used to constrain evolutionary status and mass. Several papers have been subsequently published (Ségransan et al. 2003, Kervella et al. 2003a, 2003b, 2004a and Di Folco et al. 2004) with important results on stellar fundamental parameters prior to the use of the dedicated VLTI light combiner: AMBER (Petrov et al. 2003). The aim of the present paper is to complete previous studies using VINCI to measure the diameter of three subgiant and giant stars which are among selected asteroseismic targets for ground-based observations and space missions: δ Eri, ξ Hya, η Boo. We perform a detailed study

Correspondence to: thevenin@obs-nice.fr

of their evolutionary status by constraining their mass, their helium content and their age. This will end the short history of the VINCI stellar diameter prospects for improving the understanding of stellar structure and evolution of stars. We first detail the characteristics of each of the three stars (Sect. 2) and then we present diameter measurements (Sect. 3) for each star. We construct models satisfying all observable constraints. We present these models (Sect. 4) and we draw some conclusions on the classification and fundamental parameters or the three stars.

2. Global characteristics of the stars

2.1. δ Eri

δ Eri (HD 23249, HR 1136, HIP 17378) has been thoroughly studied by photometry and spectroscopy and is classified as a K0 IV star (Keenan & Pitts 1980). It belongs to the group of the nearest stars with an accurate Hipparcos parallax of 110.58 ± 0.88 mas (Perryman et al. 1997). The star has been classified as weakly active and X-ray soft source (Huensch et al. 1999) after a long time of search for its activity. Wilson & Bappu (1957) concluded that a possible detection of emission in the lines H&K is "*exceedingly weak*" - so weak that it is questionable. Finally, it took more than 20 years to really detect its activity with Copernicus revealing a weak emission in MgII (Weiler & Oegerle 1979). Fisher et al. (1983) tried to detect a periodic variation in the photometric data and concluded that, if it exists, the amplitude is below ± 0.02 magnitude with a period of 10 days. They suggested that δ Eri could be classified as a RS CVn star. A RS CVn is defined as a F-G binary star having a period shorter than 14 days, with a chromospheric activity and with a period of rotation synchronized with its orbital period (Linsky 1984) then giving to the star a high rotational velocity inducing a strong activity. All of this is in contrast with the very small activity detected for δ Eri making doubtful its classification as a RS CVn star. δ Eri having a projected rotational velocity of $\mathrm{v} \sin \mathrm{i} = 1.0\,\mathrm{km\,s^{-1}}$ (de Meideros & Mayor 1999) the hypothetical RS CVn classification forces us to conclude that the binary is seen pole-on therefore explaining the lack of photometric variations and also of any variation of the radial velocity (Santos et al. 2004). In attempting to reveal the presence of a close companion around δ Eri, we set several VLTI/VINCI observations at different baselines (see Sect. 3).

We estimate its bolometric luminosity to $\mathrm{L}_\star/\mathrm{L}_\odot = 3.19 \pm 0.06$ using Alonso et al. (1999) empirical bolometric corrections (BC) for giants. We adopt Santos et al. (2004) values for the effective temperature $\mathrm{T_{eff}} = 5074. \pm 60.\,\mathrm{K}$, logarithmic surface gravity $\log g = 3.77 \pm 0.16$ and surface iron abundance $[\mathrm{Fe/H}] = 0.13 \pm 0.03$. Bouchy & Carrier (2003) have measured a large mean frequency spacing of 43.8μHz that we will try to reproduce with our model.

Table 1. Observable characteristics of the stars and best model reproducing them. The subscripts "$_{\rm ini}$" and "$_{\rm surf}$" respectively refer to initial values and surface quantities at present day. VLTI/VINCI diameter is in solar unit $D_\odot$.

	δ Eri	ξ Hya	η Boo
V	3.51 ± 0.02	3.54 ± 0.01	2.68 ± 0.01
$T_{\rm eff}$(K)	5074 ± 60	5010 ± 100	6050 ± 150
$L/L_\odot$	3.19 ± 0.06	60.7 ± 4.1	8.95 ± 0.20
$[Fe/H]_{\rm surf}$	0.13 ± 0.08	-0.04 ± 0.12	0.24 ± 0.07
$\log g$	3.77 ± 0.16	2.93 ± 0.30	3.66 ± 0.20
VINCI($D/D_\odot$)	2.33 ± 0.03	10.3 ± 0.3	2.681 ± 0.053
$\Delta\nu_0(\mu$Hz)	43.8 ± 0.3	7.1	40.47 ± 0.05

	δ Eri diffusion	δ Eri no diffusion	ξ Hya diffusion	ξ Hya no diffusion	η Boo diffusion	η Boo no diffusion
$M/M_\odot$	1.215	1.215	2.65	2.65	1.70	1.70
age of the ZAMS (Myr)	20.14	20.06	2.724	2.719	12.68	12.67
age (from ZAMS) (Myr)	6194.	6196.	509.52	505.34	2738.5	2355.
$Y_{\rm ini}$	0.28	0.28	0.275	0.275	0.260	0.260
$[Z/X]_{\rm ini}$	0.148	0.148	0.00	0.00	0.367	0.367
$T_{\rm eff}$(K)	5055.	5066.	5037.	5034.	6050.	6090.
$L/L_\odot$	3.176	3.230	61.23	61.0	8.944	8.978
$R/R_\odot$	2.328	2.337	10.30	10.30	2.728	2.697
$\log g$	3.788	3.785	2.835	2.832	3.796	3.806
$Y_{\rm surf}$	0.266	0.28	0.274	0.275	0.228	0.260
$[Z/X]_{\rm surf}$	0.123	0.148	0.00	0.00	0.303	0.367
$M_{\rm CZ}(M_\star)$	0.729	0.727	0.608	0.596	0.9994	0.9994
$R_{\rm CZ}(R_\star)$	0.475	0.475	0.422	0.417	0.8388	0.8505
$\Delta\nu_0(\mu$Hz)	45.27	44.91	7.23	7.28	41.91	42.47

2.2. ξ Hya

ξ Hya (HD 100407, HR 4450, HIP 56343) is a giant star (G7 III) which has been considered by Eggen (1977) as a spurious member of the Hyades group because it departs slightly from the regression line of giant stars in the colour diagrams (b-y,R-I) and (M_1,R-I) of that stellar group.

Its Hipparcos parallax is 25.23 ± 0.83 mas. We estimate its bolometric lumisosity to $L_\star/L_\odot = 60.7 \pm 4.1$ using BC from Alonso et al. (1999). We adopt the spectroscopic parameters derived by Mc William (1990): effective temperature $T_{\rm eff} = 5010. \pm 100.$ K, $\log g = 2.93 \pm 0.30$ and [Fe/H] $= -0.04 \pm 0.12$. The star belongs to the HR diagram at the lowest part of the giant branch corresponding to an evolved star with a mass around $3M_\odot$. Using a set of CORALIE spectra, Frandsen et al. (2002) detected solar-like oscillations showing radial modes with the largest amplitudes almost equidistant around 7.1μHz. That important detection opens the possibility to better constrain the model of that star for which the mass is not well-known.

2.3. η Boo

η Boo (HD 121370, HR 5235, HIP 67927) is a subgiant (G0 IV) spectroscopic binary (SB1) studied recently by Di Mauro et al. (2003) and Guenther (2004). Its Hipparcos parallax is 88.17 ± 0.75 mas. Having large overabundances of Si, Na, S, Ni and Fe, it has been considered as super-metal-rich by Feltzing & Gonzales (2001). We adopt here a luminosity $L_\star/L_\odot = 8.95 \pm 0.20$ using BC from Vandenberg and Clem (2003), an effective temperature $T_{\rm eff} = 6050. \pm 150.$ K representing the average of five effective temperature determinations in the [Fe/H] catalogue of Cayrel de Strobel et al. (2001) and the spectroscopic $\log g = 3.66 \pm 0.20$ and [Fe/H] $= 0.24 \pm 0.07$ from Feltzing & Gonzales (2001). To constrain the models further, we consider the large mean frequency spacing by Kjeldsen et al. (2003).

3. Diameter interferometric measurements

3.1. VINCI and the VLTI

The European Southern Observatory's Very Large Telescope Interferometer (Glindemann et al. 2000) is operated on top of the Cerro Paranal, in Northern Chile since March 2001. For the observations reported in this work, the light coming from two telescopes (two 0.35m test siderostats or VLT/UT1-UT3) was combined coherently in VINCI, the VLT Interferometer Commissioning Instrument (Kervella et al. 2000). We used a regular K band filter ($\lambda = 2.0 - 2.4$ μm) for these observations.

3.2. Data reduction

We used an improved version of the standard VINCI data reduction pipeline (Kervella, Ségransan & Coudé du Foresto 2004b), whose general principle is based on the original FLUOR algorithm (Coudé du Foresto et al. 1997). The two calibrated output interferograms are subtracted to remove residual photometric fluctuations. Instead of the classical

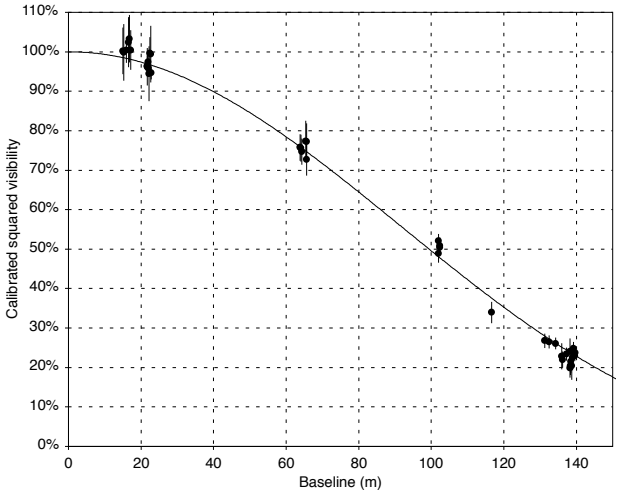


Fig. 1. Squared visibility measurements obtained on δ Eri. The solid line is a limb darkened disk model with $\theta_{\rm LD} = 2.394 \pm 0.014 \pm 0.025$ mas (statistical and systematic errors).

Fourier analysis, we implemented a time-frequency analysis (Ségransan et al. 1999) based on a continuous wavelet transform.

The differential piston strongly modifies the amplitude and the shape of the fringe peak in the wavelet power spectrum. A selection based on the shape of fringe peak in the time-frequency domain is used to remove "pistonned" interferograms. Visibilities are then derived using the wavelet power spectral density (PSD) of the interferograms. The residual photon and detector noise are removed by making a least squares fit of the PSD at high frequency.

3.3. Measured visibilities and angular diameters

The visibility values obtained on δ Eri, ξ Hya and η Boo are listed in Tables 2 to 5, and plotted on Figures 1 to 3.

The calibration of the visibilities obtained on δ Eri and η Boo was done using well-known calibrator stars that were selected in the Cohen et al. (1999) catalogue. The uniform disk (UD) angular diameter of these stars was converted into a limb darkened value and then to a K band uniform disk angular diameter using the recent non-linear law coefficients taken from Claret et al. (2000). As demonstrated by Bordé et al. (2002), the star diameters in this list have been measured very homogeneously to a relative precision of approximately 1%.

The VINCI instrument has no spectral dispersion and its bandpass corresponds to the K band filter (2-2.4 μm). It is thus important to compute the precise effective wavelength of the instrument in order to determine the angular resolution at which we are observing the targets. The effective wavelength differs from the filter mean wavelength because of

Table 2. δ Eri squared visibilities.

Julian Date	Stations	N	B (m)	Az. (deg)	$V^2 \pm$ stat $\pm$ syst	Calibrator
2452682.528	B3-D1	74	22.638	14.95	$0.9941 \pm 0.0712 \pm 0.0014$	δ Lep
2452682.541	B3-D1	460	21.963	14.63	$0.9740 \pm 0.0140 \pm 0.0014$	δ Lep
2452682.545	B3-D1	281	21.735	14.55	$0.9639 \pm 0.0264 \pm 0.0014$	δ Lep
2452682.607	B3-D1	140	16.514	14.78	$1.0242 \pm 0.0632 \pm 0.0014$	δ Lep
2452682.612	B3-D1	340	15.954	14.99	$1.0045 \pm 0.0321 \pm 0.0014$	δ Lep
2452682.618	B3-D1	133	15.285	15.27	$0.9987 \pm 0.0715 \pm 0.0013$	δ Lep
2452671.562	B3-D1	233	22.437	14.84	$0.9960 \pm 0.0409 \pm 0.0031$	δ Lep
2452671.567	B3-D1	95	22.164	14.71	$0.9442 \pm 0.0697 \pm 0.0029$	δ Lep
2452671.574	B3-D1	210	21.749	14.55	$0.9623 \pm 0.0474 \pm 0.0030$	δ Lep
2452671.631	B3-D1	397	17.152	14.59	$1.0042 \pm 0.0501 \pm 0.0014$	δ Lep
2452671.635	B3-D1	206	16.756	14.71	$1.0331 \pm 0.0604 \pm 0.0014$	δ Lep
2452671.651	B3-D1	237	14.947	15.44	$1.0023 \pm 0.0588 \pm 0.0014$	δ Lep
2452672.553	B3-D1	401	22.756	15.02	$0.9465 \pm 0.0164 \pm 0.0014$	δ Lep
2452672.567	B3-D1	426	22.013	14.65	$0.9585 \pm 0.0153 \pm 0.0014$	δ Lep
2452672.603	B3-D1	379	19.478	14.26	$0.9911 \pm 0.0235 \pm 0.0014$	δ Lep
2452672.607	B3-D1	237	19.086	14.28	$1.0134 \pm 0.0540 \pm 0.0015$	δ Lep
2452673.567	B3-D1	236	21.898	14.60	$0.9780 \pm 0.0322 \pm 0.0014$	δ Lep
2452673.579	B3-D1	264	21.130	14.39	$0.9940 \pm 0.0264 \pm 0.0015$	δ Lep
2452673.609	B3-D1	441	18.693	14.31	$1.0197 \pm 0.0253 \pm 0.0015$	δ Lep
2452674.527	B3-D1	262	23.527	15.78	$0.9718 \pm 0.0294 \pm 0.0014$	δ Lep
2452674.557	B3-D1	415	22.253	14.75	$0.9757 \pm 0.0241 \pm 0.0015$	δ Lep
2452674.562	B3-D1	405	22.003	14.64	$0.9833 \pm 0.0249 \pm 0.0015$	δ Lep
2452674.566	B3-D1	314	21.756	14.55	$0.9778 \pm 0.0281 \pm 0.0015$	δ Lep
2452675.547	B3-D1	432	22.640	14.95	$0.9731 \pm 0.0213 \pm 0.0014$	δ Lep
2452676.557	B3-D1	383	21.997	14.64	$0.9674 \pm 0.0203 \pm 0.0014$	δ Lep
2452676.561	B3-D1	402	21.734	14.55	$0.9813 \pm 0.0201 \pm 0.0015$	δ Lep
2452676.565	B3-D1	259	21.474	14.47	$0.9678 \pm 0.0338 \pm 0.0014$	δ Lep
2452676.590	B3-D1	447	19.612	14.26	$0.9883 \pm 0.0227 \pm 0.0014$	δ Lep
2452676.602	B3-D1	328	18.603	14.32	$0.9453 \pm 0.0318 \pm 0.0013$	δ Lep
2452677.543	B3-D1	480	22.582	14.92	$0.9651 \pm 0.0283 \pm 0.0014$	δ Lep
2452677.547	B3-D1	445	22.366	14.80	$0.9695 \pm 0.0294 \pm 0.0014$	δ Lep
2452677.551	B3-D1	256	22.137	14.70	$0.9283 \pm 0.0407 \pm 0.0013$	δ Lep
2452677.587	B3-D1	267	19.633	14.26	$1.0093 \pm 0.0407 \pm 0.0015$	δ Lep
2452677.598	B3-D1	381	18.695	14.31	$1.0013 \pm 0.0384 \pm 0.0015$	δ Lep
2452677.603	B3-D1	287	18.286	14.36	$1.0432 \pm 0.0455 \pm 0.0015$	δ Lep
2452678.537	B3-D1	230	22.746	15.02	$1.0024 \pm 0.0382 \pm 0.0014$	δ Lep
2452678.548	B3-D1	121	22.186	14.72	$0.9746 \pm 0.0520 \pm 0.0014$	δ Lep
2452678.559	B3-D1	168	21.531	14.49	$0.9900 \pm 0.0492 \pm 0.0014$	δ Lep
2452678.584	B3-D1	422	19.649	14.26	$1.0167 \pm 0.0354 \pm 0.0011$	δ Lep
2452678.593	B3-D1	150	18.893	14.29	$1.0966 \pm 0.0618 \pm 0.0012$	δ Lep
2452679.561	B3-D1	402	21.184	14.40	$0.9800 \pm 0.0353 \pm 0.0014$	δ Lep
2452679.566	B3-D1	278	20.892	14.35	$1.0211 \pm 0.0435 \pm 0.0015$	δ Lep
2452683.578	B3-D1	374	19.065	14.28	$0.9596 \pm 0.0152 \pm 0.0012$	δ Lep
2452683.582	B3-D1	449	18.708	14.31	$0.9900 \pm 0.0147 \pm 0.0013$	δ Lep
2452683.586	B3-D1	283	18.316	14.36	$0.9378 \pm 0.0232 \pm 0.0012$	δ Lep
2452683.593	B3-D1	269	17.654	14.48	$0.9915 \pm 0.0274 \pm 0.0013$	δ Lep

Table 3. δ Eri squared visibilities (continued from Table 2).

Julian Date	Stations	N	B (m)	Az. (deg)	$V^2 \pm$ stat $\pm$ syst	Calibrator
2452524.854	E0-G1	350	65.689	307.62	$0.7271 \pm 0.0400 \pm 0.0054$	70 Aql, 31 Ori
2452524.858	E0-G1	336	65.583	307.23	$0.7720 \pm 0.0464 \pm 0.0057$	70 Aql, 31 Ori
2452524.863	E0-G1	239	65.450	306.79	$0.7729 \pm 0.0521 \pm 0.0057$	70 Aql, 31 Ori
2452524.890	E0-G1	452	64.342	303.74	$0.7467 \pm 0.0329 \pm 0.0055$	70 Aql, 31 Ori
2452524.895	E0-G1	456	64.115	303.16	$0.7561 \pm 0.0336 \pm 0.0056$	70 Aql, 31 Ori
2452524.899	E0-G1	452	63.877	302.56	$0.7579 \pm 0.0332 \pm 0.0056$	70 Aql, 31 Ori
2452555.889	B3-M0	312	132.444	27.46	$0.2742 \pm 0.0150 \pm 0.0055$	δ Phe
2452555.893	B3-M0	275	131.275	27.44	$0.2769 \pm 0.0168 \pm 0.0056$	δ Phe
2452556.810	B3-M0	200	139.144	30.60	$0.2477 \pm 0.0152 \pm 0.0067$	δ Phe
2452556.817	B3-M0	395	139.500	30.10	$0.2294 \pm 0.0113 \pm 0.0062$	δ Phe
2452556.822	B3-M0	373	139.635	29.80	$0.2370 \pm 0.0117 \pm 0.0064$	δ Phe
2452564.830	B3-M0	146	138.416	28.23	$0.2047 \pm 0.0228 \pm 0.0019$	HR 8685
2452567.762	B3-M0	236	137.272	32.21	$0.2245 \pm 0.0153 \pm 0.0044$	HR 8685
2452577.789	B3-M0	173	138.926	28.46	$0.2248 \pm 0.0314 \pm 0.0070$	45 Eri, HR 2549
2452577.794	B3-M0	187	138.426	28.23	$0.2156 \pm 0.0289 \pm 0.0067$	45 Eri, HR 2549
2452213.776	UT1-UT3	73	101.996	232.98	$0.4883 \pm 0.0203 \pm 0.0102$	χ Phe
2452213.777	UT1-UT3	332	102.056	232.83	$0.5207 \pm 0.0138 \pm 0.0109$	χ Phe
2452213.791	UT1-UT3	69	102.374	231.76	$0.5089 \pm 0.0172 \pm 0.0106$	χ Phe
2452213.793	UT1-UT3	312	102.394	231.65	$0.5044 \pm 0.0150 \pm 0.0105$	χ Phe
2452578.723	B3-M0	269	135.965	33.09	$0.2393 \pm 0.0257 \pm 0.0063$	τ Cet
2452578.740	B3-M0	169	138.202	31.51	$0.2520 \pm 0.0246 \pm 0.0066$	τ Cet
2452578.745	B3-M0	74	138.752	31.02	$0.2133 \pm 0.0307 \pm 0.0056$	τ Cet
2452585.799	B3-M0	298	134.322	27.55	$0.2608 \pm 0.0134 \pm 0.0071$	τ Cet
2452601.810	B3-M0	206	116.676	28.41	$0.3674 \pm 0.0290 \pm 0.0082$	τ Cet
2452602.728	B3-M0	123	138.193	28.15	$0.2183 \pm 0.0241 \pm 0.0056$	τ Cet
2452602.742	B3-M0	396	136.193	27.73	$0.2412 \pm 0.0174 \pm 0.0062$	τ Cet

the detector quantum efficiency curve, the fiber beam combiner transmission and the object spectrum. It is only weakly variable as a function of the spectral type anyway.

To derive the effective wavelength of our observations, we computed a model taking into account the star spectrum and the VLTI transmission. The instrumental transmission of VINCI and the VLTI was first modeled taking into account all known effects and then calibrated based on several bright reference stars observations with the UTs (see Kervella et al. 2003b for details).

Taking the weighted average wavelength of this model spectrum gives an effective wavelength of $\lambda_{\rm eff} = 2.178\,\mu$m for δ Eri and η Boo. The visibility fits were computed taking into account the limb darkening of the stellar disk of each stars. We used power

Table 4. ξ Hya squared visibilities.

Julian Date	Stations	N	B (m)	Az. (deg)	$V^2 \pm$ stat $\pm$ syst	Calibrators
2452681.743	B3-D1	333	23.650	27.39	$0.9539 \pm 0.0376 \pm 0.0008$	α Crt
2452681.747	B3-D1	460	23.727	26.48	$0.9520 \pm 0.0305 \pm 0.0008$	α Crt
2452681.751	B3-D1	343	23.801	25.51	$0.9281 \pm 0.0334 \pm 0.0007$	α Crt
2452681.777	B3-D1	452	23.995	20.50	$0.9555 \pm 0.0304 \pm 0.0008$	α Crt
2452681.781	B3-D1	332	23.989	19.60	$0.9383 \pm 0.0337 \pm 0.0008$	α Crt
2452681.785	B3-D1	427	23.975	18.89	$0.9424 \pm 0.0305 \pm 0.0008$	α Crt
2452682.729	B3-D1	354	23.407	29.82	$0.9560 \pm 0.0251 \pm 0.0009$	α Crt
2452682.752	B3-D1	295	23.846	24.85	$0.9519 \pm 0.0280 \pm 0.0009$	α Crt
2452682.792	B3-D1	297	23.904	17.19	$0.9420 \pm 0.0317 \pm 0.0007$	α Crt
2452682.801	B3-D1	403	23.773	15.47	$0.9351 \pm 0.0237 \pm 0.0007$	α Crt
2452760.583	B3-M0	350	138.521	60.37	$0.2383 \pm 0.0058 \pm 0.0069$	α Crt
2452760.600	B3-M0	343	136.690	63.11	$0.2520 \pm 0.0061 \pm 0.0073$	α Crt
2452760.605	B3-M0	391	135.918	63.96	$0.2568 \pm 0.0059 \pm 0.0075$	α Crt
2452760.635	B3-M0	433	129.762	68.49	$0.2971 \pm 0.0058 \pm 0.0077$	α Crt
2452760.640	B3-M0	388	128.458	69.20	$0.2978 \pm 0.0061 \pm 0.0077$	α Crt
2452760.645	B3-M0	284	127.037	69.92	$0.3221 \pm 0.0071 \pm 0.0084$	α Crt
2452761.624	B3-M0	429	131.833	67.24	$0.2714 \pm 0.0063 \pm 0.0097$	51 Hya
2452761.628	B3-M0	303	130.716	67.94	$0.2787 \pm 0.0077 \pm 0.0100$	51 Hya
2452761.665	B3-M0	421	119.296	73.16	$0.3592 \pm 0.0063 \pm 0.0131$	51 Hya
2452761.671	B3-M0	402	117.300	73.87	$0.3681 \pm 0.0067 \pm 0.0135$	51 Hya
2452761.675	B3-M0	340	115.485	74.49	$0.3727 \pm 0.0087 \pm 0.0136$	51 Hya
2452762.604	B3-M0	470	135.192	64.66	$0.2554 \pm 0.0021 \pm 0.0092$	51 Hya
2452762.609	B3-M0	454	134.296	65.44	$0.2600 \pm 0.0022 \pm 0.0094$	51 Hya
2452762.614	B3-M0	386	133.310	66.21	$0.2689 \pm 0.0049 \pm 0.0097$	51 Hya
2452762.623	B3-M0	441	131.274	67.59	$0.2771 \pm 0.0027 \pm 0.0100$	51 Hya

Table 5. η Boo squared visibilities.

Julian Date	Stations	N	B (m)	Az. (deg)	$V^2 \pm$ stat $\pm$ syst	Calibrators
2452760.684	B3-M0	131	134.046	64.22	$0.3167 \pm 0.0187 \pm 0.0119$	α Crt
2452760.696	B3-M0	50	136.318	63.31	$0.3227 \pm 0.0415 \pm 0.0121$	α Crt
2452763.693	B3-M0	187	137.132	62.88	$0.3095 \pm 0.0092 \pm 0.0064$	μ Vir

law intensity profiles derived from the limb darkening models of Claret (2000) in the K band.

The resulting limb darkened diameters for the three program stars are given in Table 1.

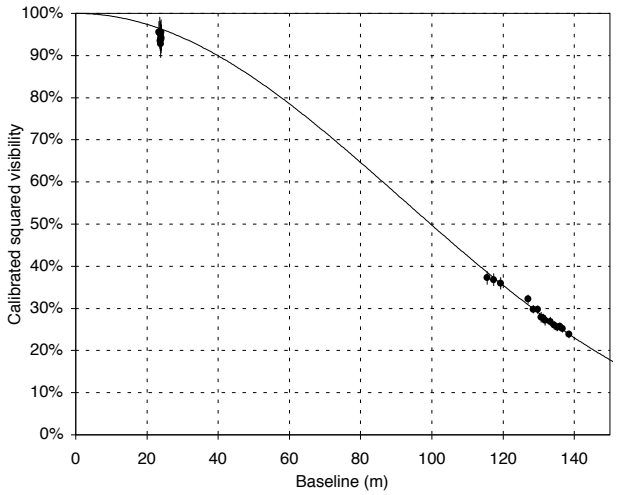


Fig. 2. Squared visibility measurements obtained on ξ Hya. The solid line is a limb darkened disk model with $\theta_{\rm LD} = 2.386 \pm 0.009 \pm 0.019$ mas (statistical and systematic errors).

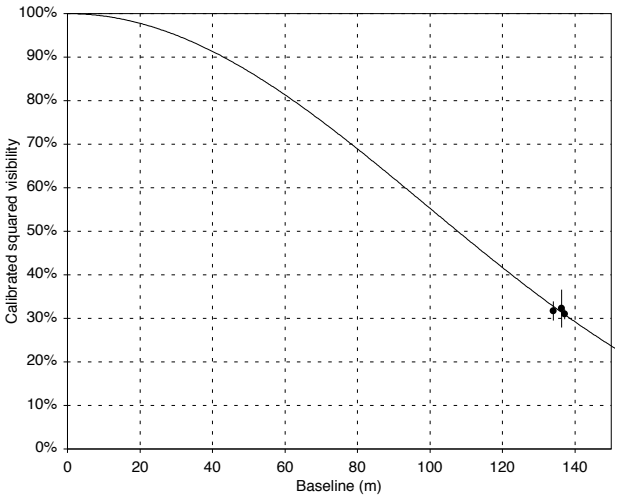


Fig. 3. Squared visibility measurements obtained on η Boo. The solid line is a limb darkened disk model with $\theta_{\rm LD} = 2.200 \pm 0.027 \pm 0.016$ mas (statistical and systematic errors).

3.4. Search for a companion to δ Eri

δ Eri is classified as a RS CVn variable (Kholopov et al. 1998), and has shown a small amplitude photometric variability (m_V = 3.51 to 3.56). Fisher et al. (1983) have also reported photometric variations with an amplitude $\Delta m_V = 0.02$ over a period of 10 days. This small amplitude and the apparent absence of periodical radial velocity modulation lead these authors to propose that δ Eri is a close binary star seen nearly pole on ($i \leq$ 5 deg). Following this idea, we can suggest three hypothesis to explain the observed photometric variations:

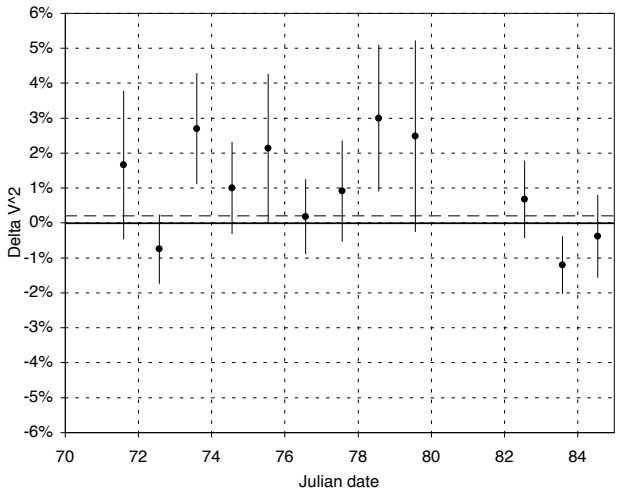


Fig. 4. Observed deviation of the squared visibilities of δ Eri (B3-D1 baseline only) with respect to the visibility model of a $\theta_{\rm UD} = 2.394$ mas uniform disk model. The dashed line represents the average deviation over all observations (0.21%).

1. The main star is ellipsoidal. This would result in a modulation of its projected surface along the line of sight during its rotation. This deformation would be caused by the close gravitational interaction of the main star with the unseen companion.
2. The companion creates a hot spot on the hemisphere of the main star that is facing it. It is changing in apparent surface when the system rotates, probably synchronously.
3. The pole of the main component holds a dark spot that is changing in apparent surface during the rotation of the star.

The period of the photometric variations, if attributed to the presence of an orbiting companion, allows to deduce the distance between the two components through the third Kepler's law. At the distance of δ Eri, this corresponds to an angular separation of approximately 9 mas, easily resolvable using moderately long baselines of the VLTI. Using the B3-D1 stations of the VLTI, we have taken advantage of the fact that the azimuth of the projected baseline is almost constant for observations of δ Eri to monitor the evolution of its visibility over a period of 13 nights. The projected length is also very well suited to the expected separation. Our interferometric data (Fig. 4) does not show any systematic deviation from the uniform disk model fit obtained using the longer baselines, at a level of $0.2 \pm 0.3\%$, consistent with zero. From these measurements, we conclude that no companion is detected at a level of about $\pm 2\%$ of the luminosity of the primary star. This result is consistent with the fact that δ Eri does not deviate significantly from the surface-brightness relations determined by Kervella et al. (2004c).

4. Models and results

The parameters used to construct our CESAM (Morel 1997) evolutionary models are summarized in Table 1. The convection is described by Canuto & Mazitelli's theory (1991, 1992) and the atmospheres are restored with Kurucz's models (1992). The other input physics are identical to those adopted for the star Procyon (see Kervella et al. 2004a). The adopted metallicity Z/X, which is an input parameter for the evolutionary computations, is given by the iron abundance measured in the atmosphere with the help of the following approximation: $\log(\frac{\mathrm{Z}}{\mathrm{X}}) \simeq [\mathrm{Fe/H}] + \log(\frac{\mathrm{Z}}{\mathrm{X}})_\odot$. We use the solar mixture of Grevesse & Noels (1993): $\left(\frac{Z}{X}\right)_\odot = 0.0245$.

The evolution tracks are initialized at the Pre-Main Sequence stage. Note that the age is counted from the ZAMS. In CESAM, the ZAMS is defined as the stage of the end of the Pre-Main Sequence where the gravitational energy release is equal to the nuclear one. We have computed models with and without microscopic diffusion of chemical species.

In asteroseismic analysis, the large frequency spacing is defined as the difference between frequencies of modes with consecutive radial order n: $\Delta\nu_\ell(n) \equiv \nu_{n,\ell} - \nu_{n-1,\ell}$ and is related to the mean density of the star.

To fit observational data (effective temperature $\mathrm{T_{eff}}$, luminosity L and surface metallicity $[\mathrm{Z/X}]_{\mathrm{surf}}$) with corresponding results of various computations, we adjust the main stellar modeling parameters: mass, age, initial helium content and metallicity.

The new measures of diameters are used to discriminate our models (see Table 1). Our best model is designed as the one which satisfies first the luminosity and radius constraint and second the effective temperature constraint. On the zooms of the HR diagrams (see Figures 6, 8, 10 and 12), the measured radius and its confidence interval appear as diagonal lines. We notice that the addition of the radius measurement reduces significantly the uncertainty domain, and in some cases tightens the allowed range for ages by a factor three (see below). We have computed models that include overshooting of the convective core (radius R_{co}) over the distance $O_{\mathrm{v}} = A_{ov} \min(H_{\mathrm{p}}, R_{\mathrm{co}})$ where R_{co} is the core radius, following the prescriptions of Schaller et al. (1992).

4.1. δ Eri

First, we adopt an initial helium content similar to the Sun $\mathrm{Y_{ini}} = 0.28$ and $[\mathrm{Z/X}]_{\mathrm{ini}} = 0.148$, both stars having similar ages and abundances (this will be confirmed hereafter).

Then, with mass and metallicity as free parameters, we have computed a grid of evolutionary tracks in order to reproduce observational data. Our best model without diffusion and without overshooting gives: $\mathrm{M} = 1.215\,\mathrm{M}_\odot$ and an age (from the ZAMS) of 6196. Myr. Our best model with diffusion and an overshooting value of $A_{ov} = 0.15$ in agreement with the results of Ribas et al. (2000) gives: $\mathrm{M} = 1.215\,\mathrm{M}_\odot$, an age (from the ZAMS) of 6194. Myr and a diameter of $\mathrm{D} = 2.328\,\mathrm{D}_\odot$. See Figures 5 and 6.

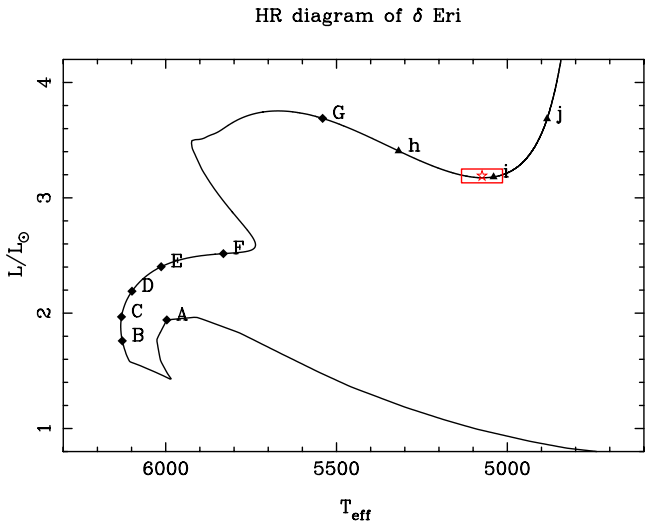


Fig. 5. Evolutionary tracks in the H-R diagram for δ Eri from label 'A' (0. Myr) to label 'G' (6000. Myr), shown by upper case letters and squares with time steps of 1000. Myr; from label 'h' (6100. Myr) to label 'j' (6300. Myr), shown by lower case letters and triangles with time steps of 100. Myr.

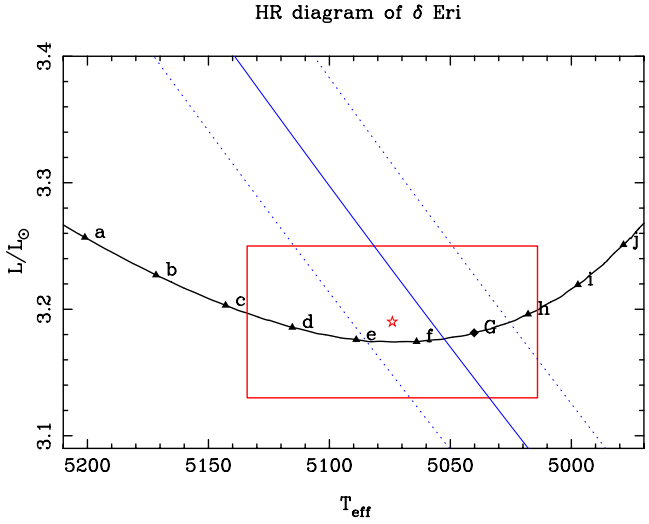


Fig. 6. Zoom of the evolutionary tracks in the H-R diagram for δ Eri from label 'a' (6140. Myr) to label 'j' (6230. Myr), shown by lower case letters and triangles with time steps of 10. Myr (except label 'G' at 6200. Myr shown by an upper case letter and a square). Our best model is close to label 'f' at 6194. Myr (see table 1).

Asteroseismic observations of δ Eri have been reported by Carrier et al. (2003) indicating an average large splitting of 43.8 μHz. For our best model, the mean large spacing is found to be 45.27 μHz in agreement within two percent of the up-to-date observations.

4.2. ξ Hya

We have computed a grid of evolutionary tracks (with and without diffusion) in order to reproduce observational data. Hence, we derived the following parameters: $M = 2.65\,M_{\odot}$

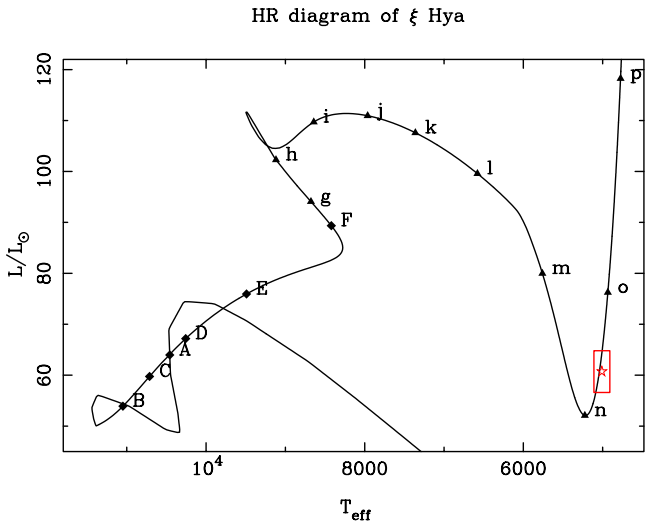


Fig. 7. Evolutionary tracks in the H-R diagram for ξ Hya from label 'A' (0. Myr) to 'F' (500. Myr), shown by upper case letters and squares with time steps of 100. Myr; from label 'g' (502. Myr) to 'p' (511. Myr), show by lower case letters and triangles with time steps of 1. Myr.

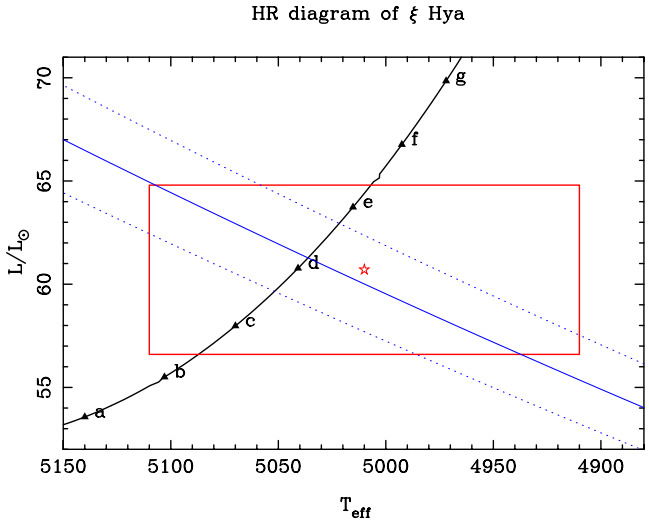


Fig. 8. Zoom of the evolutionary tracks in the H-R diagram for ξ Hya. from label 'a' (509.2 Myr) to 'g' (509.8 Myr), shown by lower case letters and triangles with time steps of 0.1 Myr. Our best model is close to label 'd' at 509.5 Myr (see table 1).

, $Y_{ini} = 0.275$ and $[Z/X]_{ini} \equiv 0.0$. Our best model with diffusion and an overshooting value of $A_{ov} = 0.20$ in agreement with the results of Ribas et al. (2000) gives us an age (from the ZAMS) of 509.5 Myr and a diameter of $D = 10.3\,D_{\odot}$. To improve the modeling, a better precision of the diameter is required as it is done for dwarf stars, for which the accuracy is better by an order of magnitude. See Figures 7 and 8.

Solar-like oscillations of that star were discovered by Frandsen et al. (2002) with a mean spacing of 7.1 μHz. From our model, we computed a value of 7.2 μHz similar to the theoretical value presented by the previous authors.

4.3. η Boo

Concerning the values of $T_{\rm eff}$ and its corresponding uncertainty, we have chosen conservative values based upon various and discrepancy determinations: Feltzing & Gonzales (2001) gives $T_{\rm eff} = 6000. \pm 100.$ K whereas Cayrel de Strobel (2001) gives a range between 5943. et 6219. K . We notice that DiMauro et al. adopt $T_{\rm eff} = 6028. \pm 45.$ K but in our study, we take advantage of the constraint given by the new diameter value which reduces the uncertainty as shown on Figures 10 or 12.

In a first attempt to characterize this star, DiMauro et al. (2003) propose to limit the range of mass between $1.64\,M_\odot$ and $1.75\,M_\odot$. Recently, Guenther (2004) adopted in his conclusion a mass of $1.706\,M_\odot$ with an initial chemical composition: $X_{\rm ini} = 0.71$, $Y_{\rm ini} = 0.25$ and $Z_{\rm ini} = 0.04$. In the present study, we have computed a grid of models and it appears that the best fitting parameters are: $M = 1.70\,M_\odot$ with an initial chemical composition: $X_{\rm ini} = 0.70$, $Y_{\rm ini} = 0.26$ and $Z_{\rm ini} = 0.04$. A first set of models have been computed with the simplest available but reliable physics (and therefore without diffusion, as probably done by the previous cited authors). A second set of models have also been computed with improved physics. Thus, we include convective overshooting (with $A_{ov} = 0.15$, see previous discussion), diffusion and radiative diffusivity (see Morel & Thévenin 2002) which controls diffusion of chemical elements in intermediate mass stars. The two sets of results give evidently similar results except concerning the ages: the age of the best model with diffusion (2738.5 Myr) is larger than the age of the best model without diffusion (2355.0 Myr).

As shown, for example, on Figure 10, without the constraint given by diameter, the age will be ranging from 2295. Myr (between label 'b' and label 'c') to 2410. Myr (close to label 'n'), with a derived uncertainty of 115. Myr. Due to the constraint on diameter, the age will be ranging from 2323. Myr (close to label 'e') to 2370. Myr (close to label 'j'), with a derived uncertainty reduced to only 47. Myr (Figures 9, 10, 11 and 12).

5. Concluding remarks

We have measured with the instrument VLTI/VINCI the diameters of three subgiant and giant stars and used them as an additive constraint to the spectro-photometric and asteroseismic ones to perform a study of their evolutionary status.

Owing the position of the three stars in the HR diagram, we can notice that the determination of the modeling parameters, in particulary the age, is very sensitive to the input physics, due to the rapidity of the stellar evolution compared to the size of the error boxes.

δ Eri is a star at the end of the subgiant phase ($M = 1.215\,M_\odot$) with an age of 6.2 Gyr. We attempt without success to detect a close companion forcing us to conclude that the classification of δ Eri as a RS CVn star is doubtful.

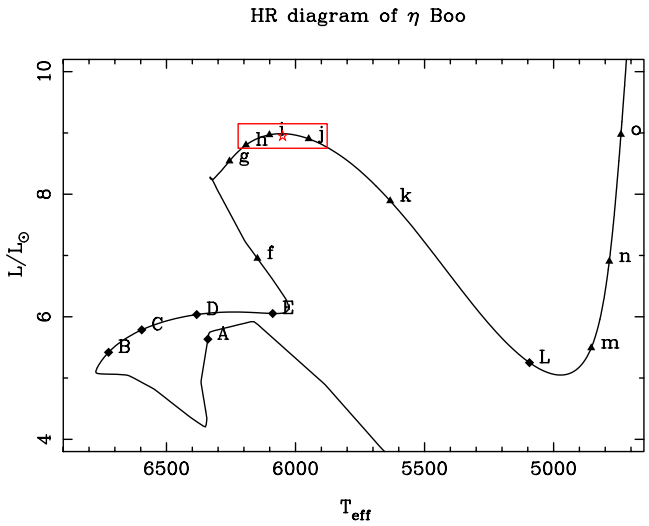


Fig. 9. Evolutionary tracks in the H-R diagram for η Boo (model without diffusion) from label 'A' (0. Myr) to 'E' (2000. Myr), shown by upper case letters and squares with time steps of 500. Myr; from label 'f' (2200. Myr) to 'o' (2650. Myr), shown by lower case letters and triangles with time steps of 50. Myr (except label 'L' at 2500. Myr shown by an upper case letter and a square).

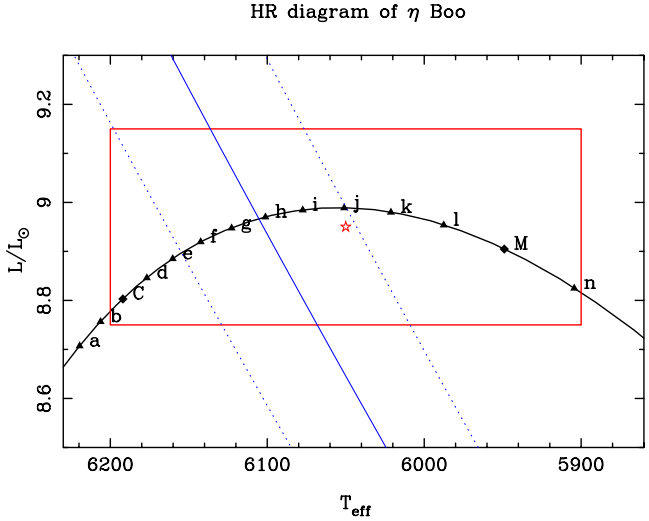


Fig. 10. Zoom of the evolutionary tracks in the H-R diagram for η Boo (model without diffusion) from label 'a' (2280. Myr) to 'n' (2410. Myr), shown by lower case letters and triangles with time steps of 10. Myr (except labels 'C' at 2300. Myr and label 'M' a 2400. Myr shown by an upper case letters and squares). Our best model is close to label 'h' at 2350. Myr (see table 1).

ξ Hya has been constrained with success with a model adopting a mass of 2.65 $M_\odot$ and an age of 510. Myr.

η Boo is a subgiant slightly more evolved than Procyon with a similar age of 2.7 Gyr. With a mass found at M = 1.7 $M_\odot$ (similar to the mass adopted by Di Mauro et al. (2003)), we were able to reproduce the VLTI/VINCI radius. In consequence, the models of Di Mauro et al. with the largest radius and oldest age are therefore questionable.

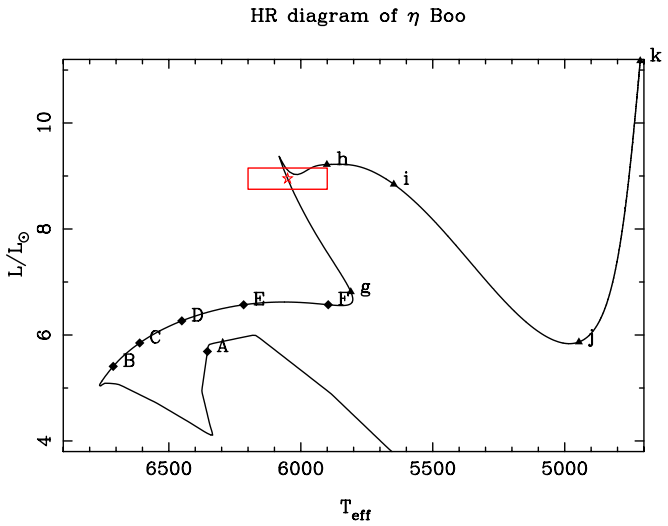


Fig. 11. Evolutionary tracks in the H-R diagram for η Boo (model with diffusion) from label 'A' (0. Myr) to label 'F' (2500. Myr), shown by upper case letters and squares with a time step of 500. Myr; label 'g' at 2700. Myr shown by a triangle; from label 'h' (2750. Myr) to label 'k' (2900. Myr), shown by lower case letters and triangles with a time step of 50. Myr.

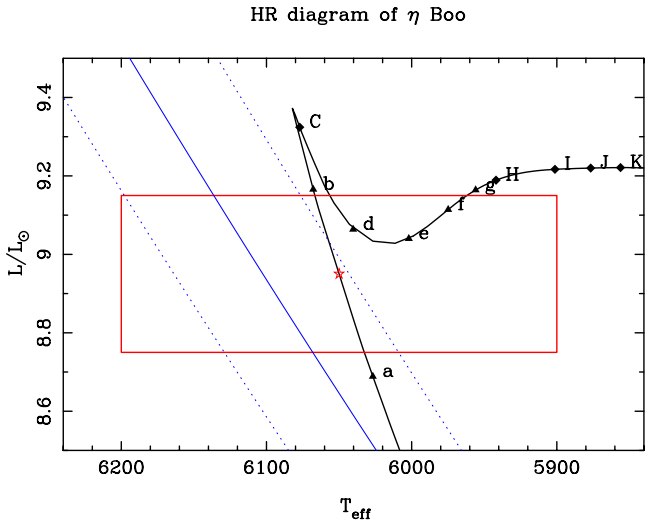


Fig. 12. Zoom of the evolutionary tracks in the H-R diagram for η Boo (model with diffusion) from label 'a' (2738. Myr) to label 'g' (2744. Myr), shown by lower case letters and triangles with time steps of 1. Myr (except label 'C' at 2740. Myr shown by a square); from label 'H' (2745. Myr) to label 'K' (2760. Myr), shown by upper case letters and squares with time steps of 5. Myr. Our best model is between label 'a' (at 2738. Myr) and label 'b' (at 2739. Myr) (see table 1).

Some progress on the asteroseismic observations are now required to better constrain the evolution state of giant stars for which the frequency spacings (Bouchy & Carrier 2003) are still relatively imprecise. The improvement of the angular diameter estimations in the future will further tighten the uncertainty domain on the HR diagram, especially as

detailed modeling of the atmosphere will be required. This improvement will naturally require a higher precision on the parallax value to derive the linear diameters.

Acknowledgements. The VINCI public commissioning data reported in this paper has been retrieved from the ESO/ST-ECF Archive. The VINCI pipeline includes the wavelets processing technique, developed by D. Ségransan (Obs. de Genève). No VLTI observation would have been possible without the efforts of the ESO VLTI team, to whom we are grateful. This work has been performed using the computing facilities provided by the program Simulations Interactives et Visualisation en Astronomie et Mécanique (SIVAM) at the computer center of the Observatoire de la Côte d'Azur. This research has made use of the Simbad database operated at CDS, Strasbourg, France.

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